

Jasmin Katz

London School of Economics

ZERO-SUM RAMSEY NUMBERS OF BOUNDED DEGREE GRAPHS

Zero-sum Ramsey numbers were defined by Bialostocki and Dierker in 1990 as an algebraic variant of the well-known Ramsey number. Given a graph G and a finite Abelian group $(\Gamma, +)$ such that $|\Gamma|$ divides $e(G)$, the *zero-sum Ramsey number* of G in Γ , denoted by $R(G, \Gamma)$, is the minimum integer t such that for any edge-colouring $c : E(K_t) \rightarrow \Gamma$, there is a copy G' of G in K_t such that $\sum_{e \in E(G')} c(e) = 0_\Gamma$.

We prove that a linear upper bound of the form $R(G, \Gamma) \leq Cn$ holds for every bounded degree n -vertex graph G and finite Abelian group Γ , where $|\Gamma|$ divides $e(G)$. Here C depends only on the maximum degree of G . This bound is tight up to the value of the multiplicative constant.

This is joint work with Xiaopan Lian, Alexandru Malekshahian, and Andrey Shapiro.